

Using expert's knowledge in Bayesian analysis

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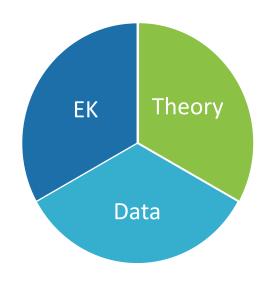
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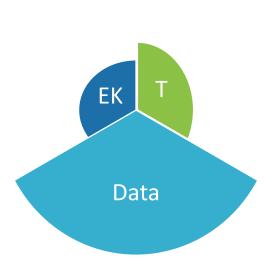
http://www.cec.lu.se/ullrika-sahlin

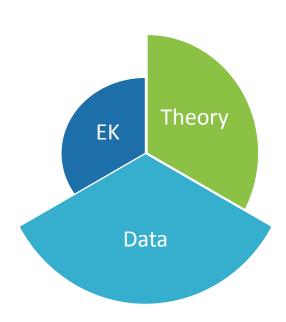


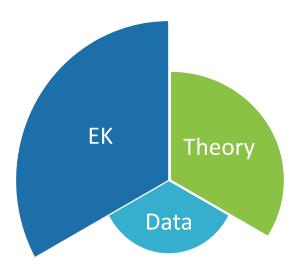






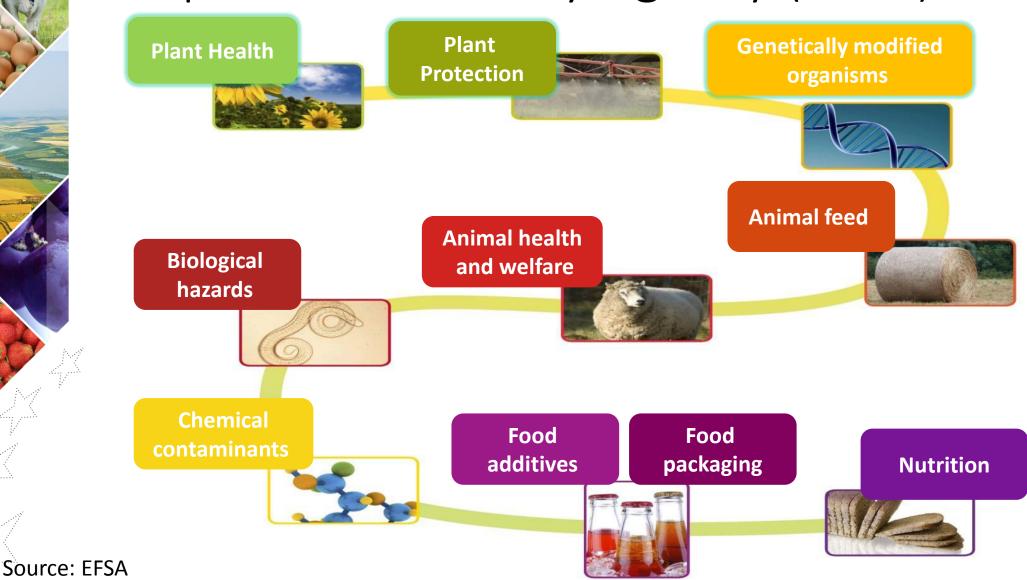






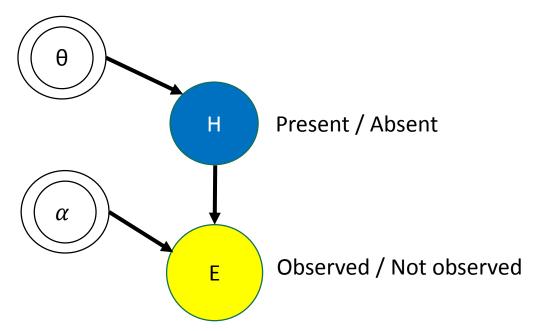


European Food Safety Agency (EFSA)



Is the crayfish still present?



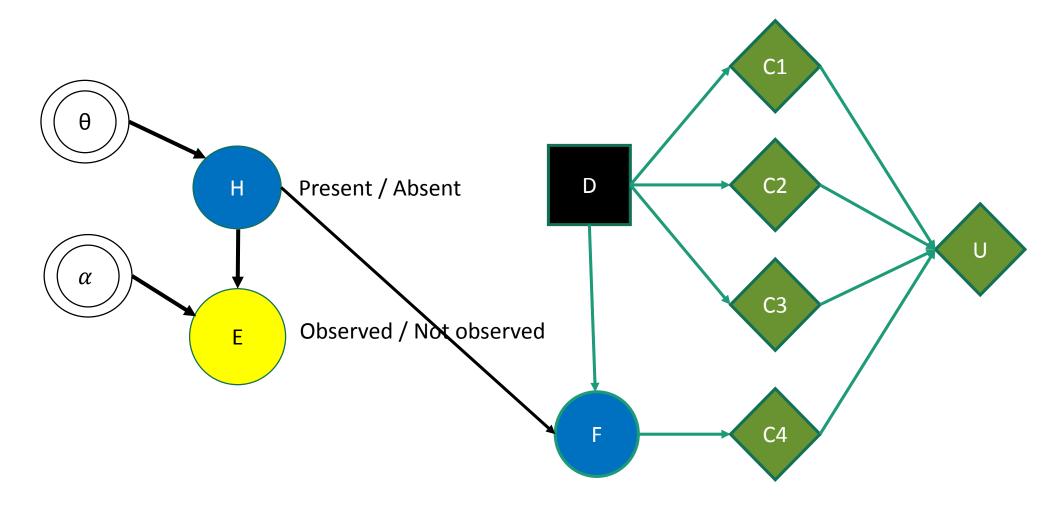


Н	
Present	θ
Absent	$1 - \theta$

	Н		
E	Present	Absent	
Observed	α	0	
Not observed	$1-\alpha$	1	

$$P(H|not E) = \frac{(1-\alpha)\theta}{1-\alpha\theta}$$

What to do with the crayfish?



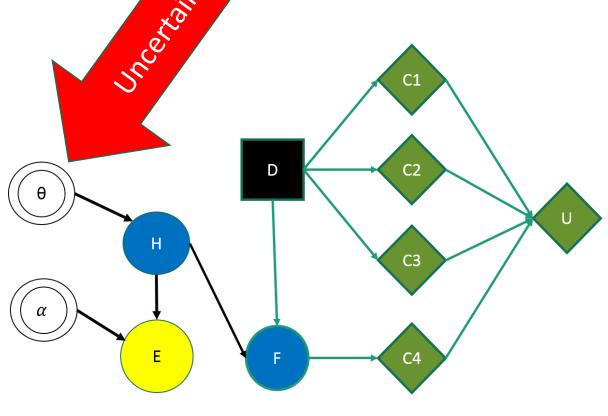
What to do with the crayfish?





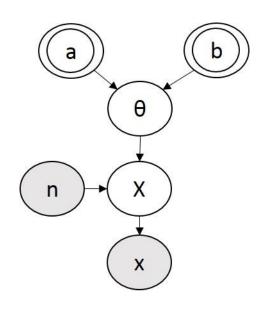


Management alternative	C1: Cost	C2: Neg Impact	C3: Accept- ance
Do nothing	0	0	0
Mechanical removal	10	2	10
Add poison	5	10	2



C4: Loss is even worse if crayfish is present after management





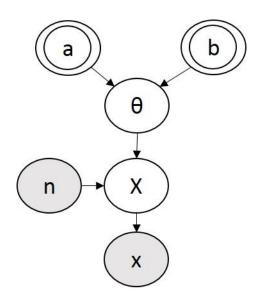
 θ parameter of interest

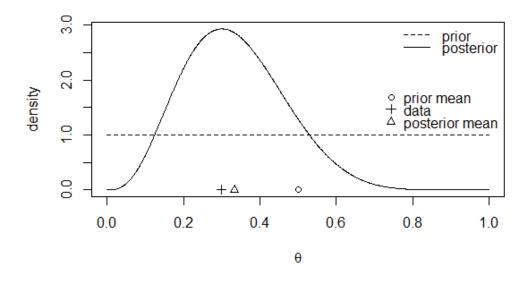
a & b expert knowledge on θ

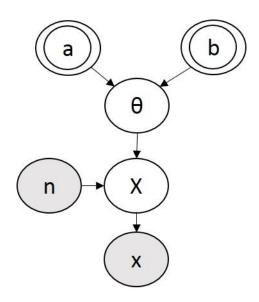
X system variable

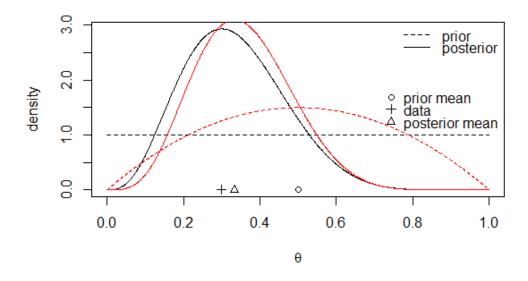
n sample size

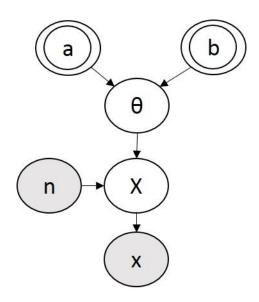
x observations of the variable

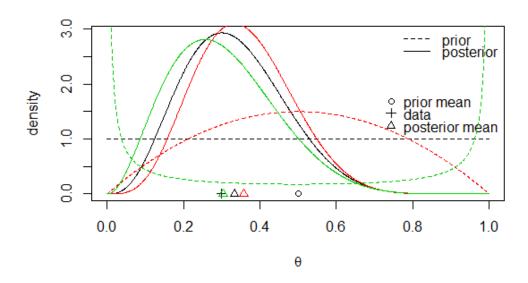








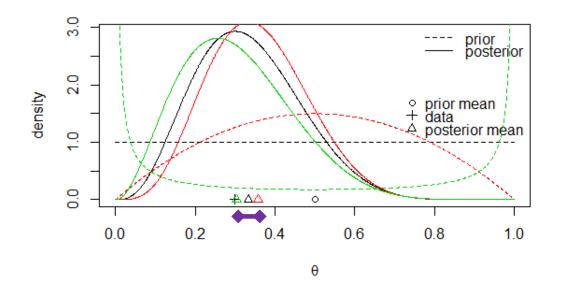


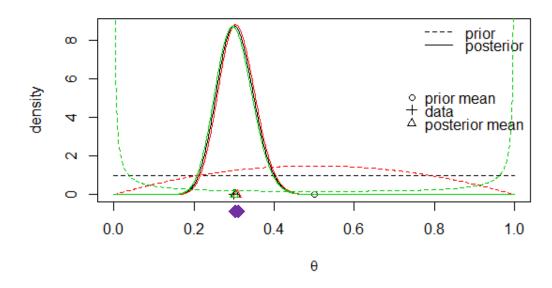


The prior may matter – better get it right

Small sample size

Large sample size









EK in risk and decision analysis

Quantitative risk models should be informed by systematically reviewed scientific evidence, however, in practice empirical evidence is often limited: in such cases it is necessary to turn to expert judgement.

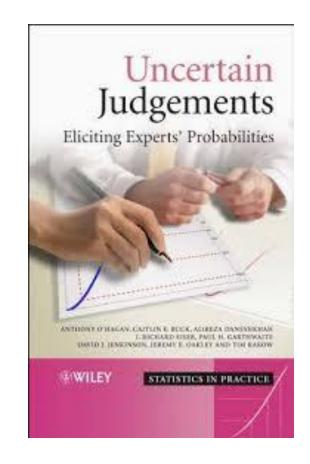
Psychological research has shown that unaided expert judgement of the quantities required for risk modelling - and particularly the uncertainty associated with such judgements - is often biased, thus limiting its value.

Accordingly methods have been developed for eliciting knowledge from experts in as unbiased a manner as possible.

Expert's Knowledge Elicitation

- Aim to describe the Expert's Knowledge about one or more uncertain quantities in probabilistic form
- i.e. a joint probability distribution for the random variable in question

 EKE can be used to build priors distributions or prior predictive distributions





An Expert Knowledge Elicitation

- Formulate the elicitation questions
- Ask experts about
 - Probabilities
 - Quantiles
 - Probability intervals
 - Moments or other descriptions of a probability distribution
- Fit and aggregate into a probability distribution for the uncertain quantity

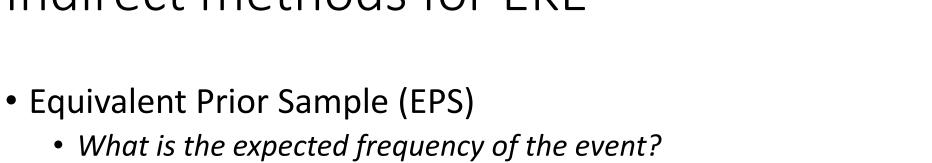


Direct methods for EKE

- Simple and a bit crude
 - Intervals Lower and Upper limits, then a Uniform distribution
 - Triangular distributions Mode, Lower and Upper limits
- Cumulative Density Function (CDF)
 - Quartiles 4 intervals, median and 25th and 75th percentiles
 - Tertiles 3 intervals with equal probability
 - Probabilities/Hybrid Choose probabilites and intervals
- Probability Density Function (PDF)
 - Mode/Mean, percentiles, shape,...
 - Place chips, draw it by hand...



Indirect methods for EKE



• What is the size a sample that you imagine to have behind this estimate?

$$\frac{x}{n} = ?$$
 $n = ?$

- Hypothetical Future Sample (HFS)
 - In a future sample of size 100 in how many times has the event occured?

$$n = 100$$
 $x = ?$



Selection of Structured EKE Software

- EXCALIBUR (EXpert CALIBration): www.lighttwist.net/wp/excalibur
- ElicitN: www.downloadcollection.com/elicitn.htm
- SHELF (The SHeffield Elicitation Framework): www.tonyohagan.co.uk/shelf/
- MATCH Uncertainty Elicitation
 Tool: optics.eee.nottingham.ac.uk/match/uncertainty.php#
- UncertWeb The Elicitator: http://elicitator.uncertweb.org/
- Variogram elicitation: <u>www.variogramelicitation.org</u>
- Unicorn: www.lighttwist.net/wp/unicorn-download



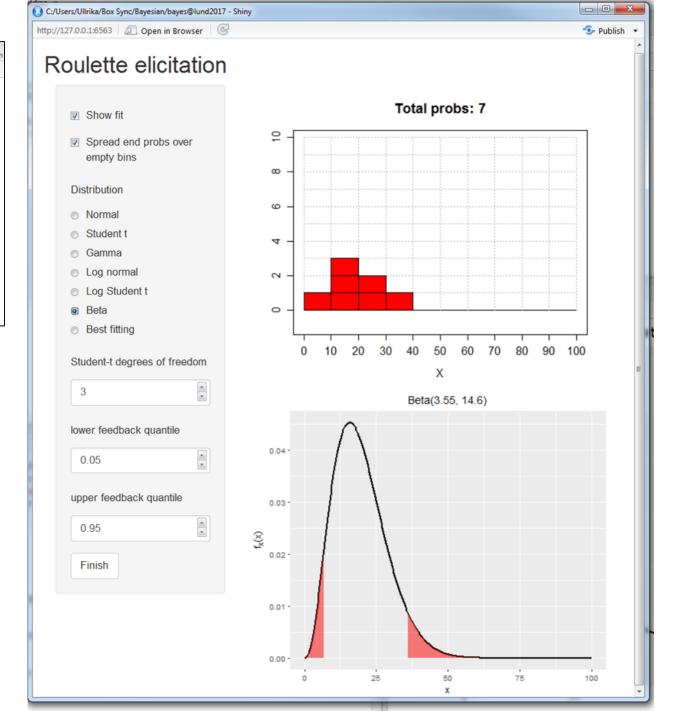
An example

 elicit the probability of the crayfish individuals to survive the winter



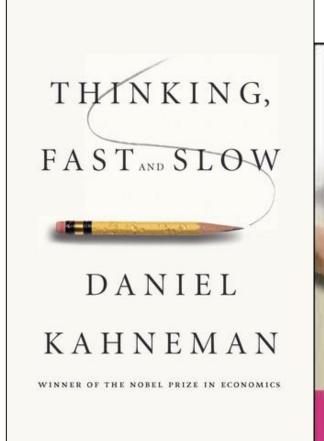
- The SHELF R-package
- A web-interface for the SHELF R-package: <u>optics.eee.nottingham.ac.uk/match/uncertainty.php#</u>
- Roulette
- Quartiles
- Tertile

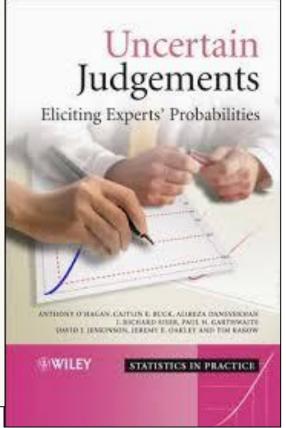
```
EK.R ×
Run Source •
 3 ## elicit one expert or consensus distribution
4 EK_info <- roulette(lower = 0, upper = 100, gridheight = 10, nbins = 10)</pre>
  6 EK_info
 7 $v
  8 [1] 10 20 30 40 50 60 70 80 90 100
10 $p
 11 [1] 0.1428571 0.5714286 0.8571429 1.0000000 1.0000000 1.0000000 1.0000000 1.0000000
12 [10] 1.0000000
 13
14 ## fit distribution to expert info
15 EK <- fitdist(vals = EK_info$v, probs = EK_info$p, lower = 0, upper = 100)
17 plotfit(EK, ql = 0.05, qu = 0.95, d = "beta")
 18
19
```



Pshycological factors and elicitation

- Anchoring and adjustment
- Availability
- Range—frequency compromise
- Representativeness and baseline neglect
- Conjuction fallacy
- The law of small numbers
- Overconfidence





Elicitation with multiple experts

Psychological factors when working with several experts

- Behavioural aggregation
 - Group elicitation
 - One or several iterations, individually and in group
- Mathematical aggregation
 - Treat each expert's distribution as data and update the decision maker's belief
 - Pooled opinions linear or logarithmic pooling
 - Calibrate experts and weight according to their performance





Alternative protocols for EKE

- the Sheffield protocol with group interaction of experts, consensus distributions
- the Cooke protocol with use of seed questions for the calibration of experts, no interaction
- a Delphi protocol on written expert elicitation with feedback loops, anonymous sharing of the results between iterations

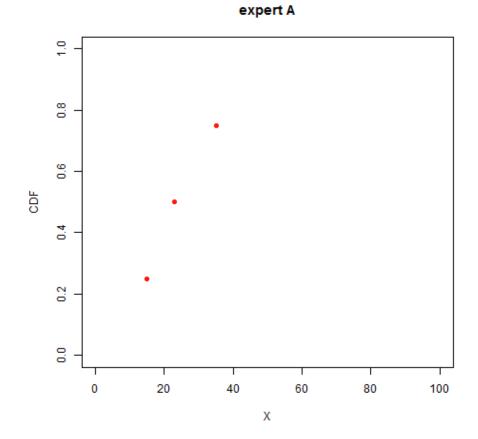


An example — elicit the probability of the crayfish individuals to survive the winter

75% percentile

Median

25% percentile





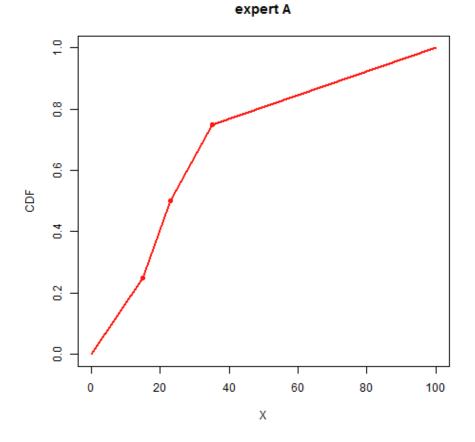


An example — elicit the probability of the crayfish individuals to survive the winter

75% percentile

Median

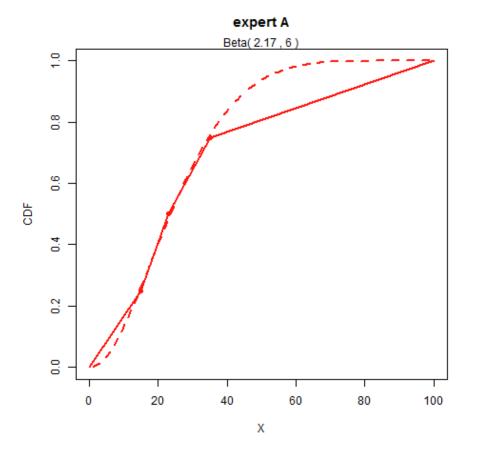
25% percentile





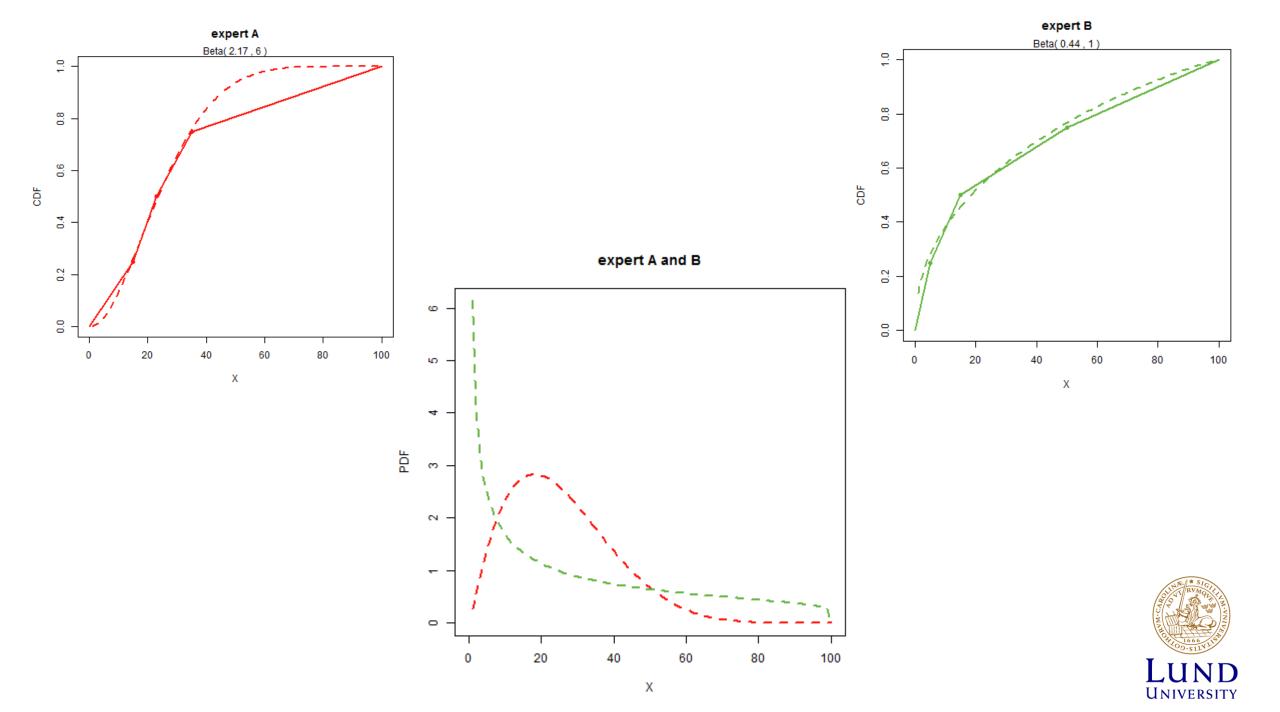


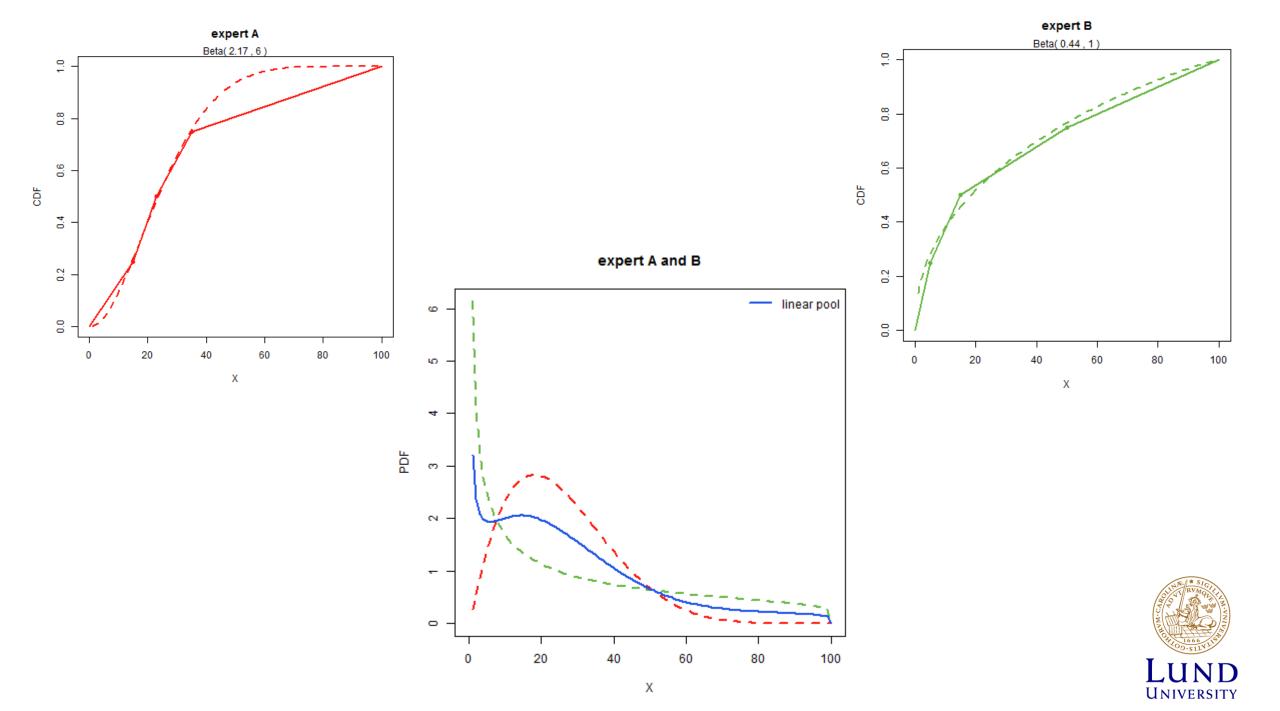
An example — elicit the probability of the crayfish individuals to survive the winter













Train the experts in making probabilistic judgments

- Get them custom to use probability density functions as a device for representing subjective uncertainty
- Clarify what is needed for the assessment, what are the uncertain quantities and how they are used to assess risk
- Reassure the experts understand that they will not be expected to claim certainty they do not have
- Encourage experts to be honest
- Give the experts a practice elicitation exercise
- Discuss psychological biases



The state of the art in expert judgment

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The benefit of quantifying uncertainty using probability

- X is the proportion surviving the first spray
- Y is the proportion surviving the second spray
- Proportion surviving both applications is XY

X is small and Y is small, what is then XY?
What does "small" mean?



The benefit of quantifying uncertainty using probability

- X is the proportion surviving the first spray
- Y is the proportion surviving the second spray
- Proportion surviving both applications is XY

X and Y without uncertainty result in a single value of XY

A false sense of security



The benefit of quantifying uncertainty using probability

- X is the proportion surviving the first spray
- Y is the proportion surviving the second spray
- Proportion surviving both applications is XY

Using point estimates in input can result in biased estimate of overall risk

Plug in estimates – no uncertainty	Consider uncertainty in inputs
E(X) = 2%	X ~ U(0,4%)
E(Y) = 2%	Y ~ U(0,4%)
XY = E(X)E(Y) = 0.04%	E(XY) = 0.053

Aleatory and epistemic uncertainty

Uncertainty in Scientific Assessment



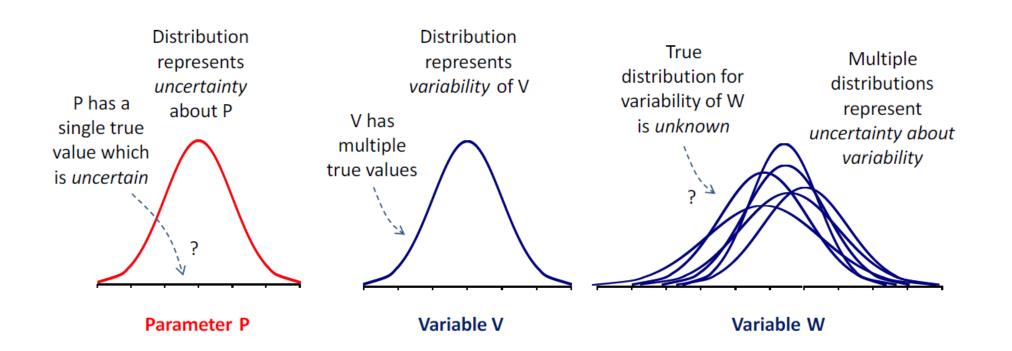


Figure 2: Illustration of the distinction between uncertainty and variability (left and central graphs), and that both can affect the same quantity (right hand graph).

